#### Potential Energy and Conservation of Energy Work Done by Gravity □ If one lifts an object of mass m from the floor $(y_i=0)$ to a height $y_f=h$ , you have done work on the object $W = F \cos \phi s = mg(y_f - y_i) = mgh$ □ We have imparted energy to it, but it is at rest (v=0). So, this energy is not kinetic energy. It is called Potential Energy (PE or U), or in this particular case, gravitational potential energy U is energy that is stored and which can be converted to another kind of energy, K for example

## $U_g = mgy$

- $\Box$  U is a scalar with units of J in S.I.
- □ y is the height above some reference point, e.g. table, floor, ...
- Conservation of (Mechanical) Energy
- Total (mechanical) energy is constant within some specified system
- total energy is conserved
- conservation principles are very important in physics; we will see many others later

# $E = K + U \ (+E_{\text{rest}})$

- E is always constant, but K and U can change
- □ If U and K change, they must change in such a way as to keep E constant

**Example** 

Consider the 1D free-fall of an object of mass m from a height of  $y_i = h$ 

 $y \uparrow m y_i=h, t_i=0, v_i=0$ 

system

The initial energy of the system defines the total energy

∎ y<h, t, v<0

$$U_i = mgh, \quad K_i = 0$$

$$E = K + U = mgh$$

System – the collection of objects being study to the exclusion of all other objects in the surroundings, in this example, we consider the object of mass m only

Some time later, K and U have changed, but E has not

$$E = K + U$$

$$mgh = \frac{1}{2}mv^{2} + mgy$$

$$K = mgh - mgy$$

$$= mg(h - y)$$
What is K, U, and v when y=h/2?

$$U = mgy = mg\frac{h}{2}, \ K = mg(h - \frac{h}{2}) = mg\frac{h}{2}$$

$$K = mg \frac{h}{2} = \frac{1}{2} mv^{2}$$

$$v = \sqrt{gh} = \sqrt{(9.80 \frac{m}{s^{2}})(1.00 \text{ m})} = 3.13 \frac{m}{s}$$

$$E = mgh = (1.00 \text{ kg})(9.80 \frac{m}{s^{2}})(1.00 \text{ m}) = 9.80 \text{ J}$$

$$U = K = mg \frac{h}{2} = \frac{E}{2} = 4.90 \text{ J}$$
For y=0 (just before the object hits the ground)?
$$U = mgy = 0, E = K = mgh = 9.80 \text{ J}$$

$$\frac{1}{2} mv^{2} = mgh$$

 $v = \sqrt{2gh} = \sqrt{2(9.80\frac{m}{s^2})(1.00 m)} = 4.43\frac{m}{s}$ 

Note: we have neglected air resistance and what happens when the object hits the ground.

#### **Example Problem**

A particle starting from point A, is projected down the curved runway. Upon leaving the runway at point B, the particle is traveling straight upward and reaches a height of 4.00 m above the floor before falling back down. Ignoring friction and air resistance, find the speed of the particle at point A.



### **Example Problem**

A grappling hook, attached to a 1.5-m rope, is whirled in a circle that lies in the vertical plane. The lowest point on this circle is at ground level. The hook is whirled at a constant rate of three revolutions per second. In the absence of air resistance, to what maximum height can the hook be cast?

Method: use concepts of conservation of mechanical energy and uniform circular motion