Tetraneutron?

Can a four-neutron, no-proton particle exist?



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- A 186 MeV/u beam of radioactive ⁸He (doublycharged) collides with normal ⁴He
- Experiments done at RIKEN Radioactive Ion Beam Factory
- Isolated neutrons have a half-life of only about
 15 minutes $n^0 \rightarrow p^+ + e^- + \bar{\nu}_e$
- Proton has a half-life of 10²⁹ years
- Bound neutron in a nucleus are stable
- Conserved properties of matter: charge, mass, quark number (proton number, neutron number), lepton number, ...

Momentum Conservation and Collisions

- Involves two (or more) objects which may have their motion (velocity, momentum) altered by collisions
- □ These concepts are applicable to the collisions of atoms, ions, billiard balls, cars, planetary objects, galaxies, etc.
- □ Say, we have a collection of interacting particles numbered 1, 2, 3, ... We can define the Total Momentum of the system (all the particles) as just the sum of all the individual momenta

$\vec{P} = \sum \vec{p}_i = \vec{p}_1 + \vec{p}_2 + \vec{p}_3 + \dots$

- □ Imagine that these particles interact in some way collide and scatter
- ❑ As long as there are no net external forces acting on the system (collection of objects), the Total Linear Momentum does not change
- □ This means: the Total Linear Momentum is the same before the collision, during the collision, and after the collision \rightarrow \rightarrow

$$\vec{P}_i = \vec{P}_f$$

Conservation of Linear Momentum

Example - 1D

A 45-kg swimmer runs with a horizontal velocity of +5.1 m/s off of a boat dock into a stationary 12-kg rubber raft. Find the velocity that the swimmer and raft would have after impact, if there were no friction and resistance due to the water.

Solution:

Given: $m_1 = 45 \text{ kg}, m_2 = 12 \text{ kg},$ $\vec{v}_{i1} = +5.1 \frac{\text{m}}{\text{s}} \hat{i}, \vec{v}_{i2} = 0$ Find: $\vec{v}_{f1}, \vec{v}_{f2} = ?$

- Consider motion of boy and raft just before and just after impact
- Boy and raft define the system
- □ Neglect friction and air resistance \rightarrow no net external forces
- Therefore, we can use the Conservation of Linear Momentum





□ What if we have the case where $v_{f1} \neq v_{f2}$? We then have two unknowns. So, we need another equation. We will return to this prob. in Chap. 10.

Problem P63 (Chapter 3)

□ Suppose that all the people of the Earth go to the • North Pole and, on a signal, all jump straight up. Estimate the recoil speed of the Earth. The mass of the Earth is 6×10^{24} kg. Problem P48 (Chapter 3) □ When they are far apart, the momentum of a proton is <3.4,0,0>x10⁻²¹ kg m/s as it approaches another proton that is initially at rest. The two protons repel each other electrically, without coming close enough to touch. When they are once again far apart, one of the protons now has a momentum <2.4,1.55,0>x10-²¹ kg m/s. At that instance, what is the momentum of the other proton?

Collisions in 2D

- Start with Conservation of Linear Momentum vector equation
- □ Similar to 2D kinematic problems: break into xand y-components $\vec{P}_i = \vec{P}_f$

$$P_{ix} = P_{fx}, \qquad P_{iy} = P_{fy}$$

Example Problem

Three guns are aimed at the center of a circle. They are mounted on the circle, 120° apart. They fire in a timed sequence, such that the three bullets collide at the center and mash into a stationary lump. Two of the bullets have identical masses of 4.50 g each and speeds of v_1 and v_2 . The third bullet has a mass of 2.50 g and a speed of 575 m/s. Find the unknown speeds.

Solution:

Given: $m_1 = m_2 = 4.50 \text{ g}, m_3 = 2.50 \text{ g},$ $v_{i3} = 575 \text{ m/s}, v_{f1} = v_{f2} = v_{f3} = 0$ Find: v_{i1} and v_{i2}

Method: If we neglect air resistance \rightarrow then there are no external forces (in the horizontal x-y plane; gravity acts in the vertical direction) \rightarrow we can use Conservation of Linear Momentum



Center of Mass

□ The average location for the total mass of a collection of particles (system)

Consider two particles located along a straight line $m_1 x_1 + m_2 x_2$



r _	$mx_1 + mx_2$	$m(x_1 + x_2)$	$x_1 + x_2$
λ_{cm} –	m+m	2m	2

Also can define the center of mass for multiple particles - N number of particles



Where M is the total mass of the system

□ Can also define the center of mass along other coordinate axes - y_{cm} and z_{cm}

Can also define the velocity of the center of mass $\mathbf{v}_{cm} = \frac{m_1 \mathbf{v}_1 + m_2 \mathbf{v}_2}{m_1 + m_2}, \text{ or } \mathbf{v}_{cm} = \frac{\sum_{j=1}^{m_j \mathbf{v}_j} m_j \mathbf{v}_j}{M}$ but $\sum m_j v_j = P = \text{total momentum}$ *j*=1 $P = Mv_{cm}$ If linear momentum is conserved, then $P_i = P_f \Rightarrow Mv_{i,cm} = Mv_{f,cm}$ $\mathbf{V}_{i,cm} = \mathbf{V}_{f,cm}$ The velocity of the center of mass is constant. It is the same before and after a collision.



Taking $x_1 = 0$ and $\Delta x = x_2 - x_1 = x_2$